

Lecture 1

04 September 2024 13:26

The Perfect Gas

N.B. : "perfect" means no interactions

"ideal" means all interactions are the same

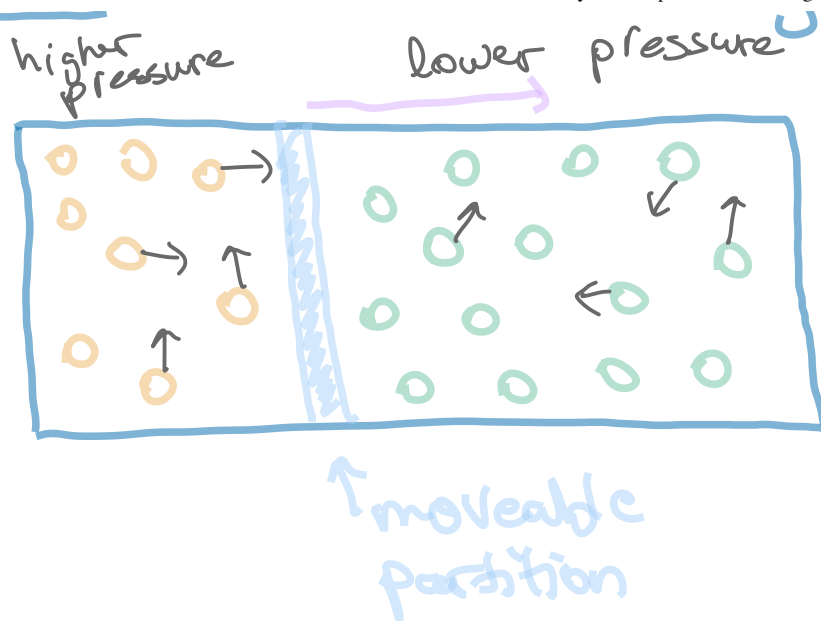
variables of state

What is a state ?

Let's suppose we have a system of three particles



Pressure : force divided by area



SI unit : pascal , Pa

$$1 \text{ Pa} = 1 \text{ N m}^{-2} = 1 \text{ kg m}^{-1} \text{ s}^{-2}$$

↳ standard state

$$p^\ominus = 1 \text{ bar}$$

Volume : the measure of the extent of space a gas occupies

SI unit : m^3

Temperature : related to the motion of molecules

Kelvin scale : absolute scale ; K

Amount : a measure of "how much"

a chemical species is present

$$N_A = 6.022 \times 10^{23} \text{ mol}^{-1}$$

Intensive vs. extensive properties

↑
does not
depend on
amount

↑
depends
on amount

e.g. T

e.g. V

molar quantities: $X_m = \frac{X}{n}$

e.g. $V_m = \frac{V}{n}$

Equation of State

$$P = f(T, V, n)$$

← where we
want to end up

Empirical Laws

Boyle's Law : $PV = \text{constant}$

Charles's Law :

(n, T constant)

$$V = \text{constant} \cdot T$$

(n, p constant)

$$p = \text{constant} \cdot T$$

(n, V constant)

Avogadro's Principle : $V = \text{constant} \cdot n$

(p, T constant)

Combining these laws, we obtain

$$pV = \text{constant} \cdot nT$$



gas constant

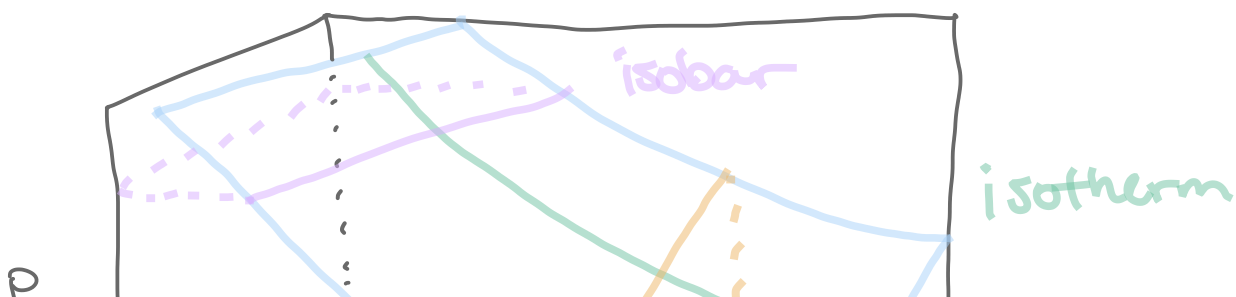
$$pV = nRT$$

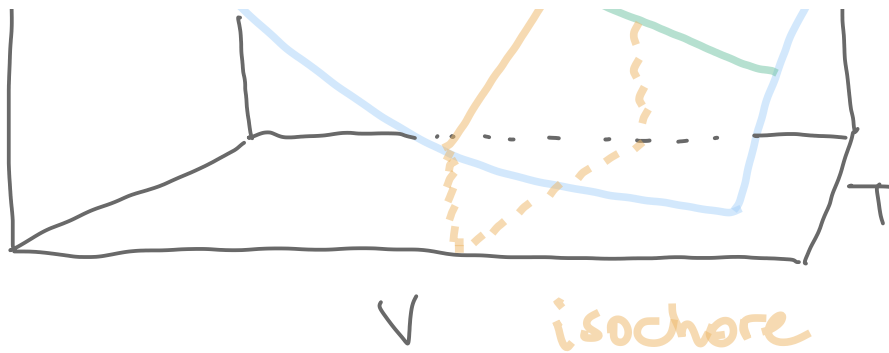
perfect gas law,

perfect gas

equation of state

$$R = k_B \cdot N_A$$





Mixtures of Gases

partial pressure :

$$P_J = x_J P$$

↑
mole fraction of
component J

$$x_J = \frac{n_J}{n}, \quad n = n_A + n_B + \dots$$

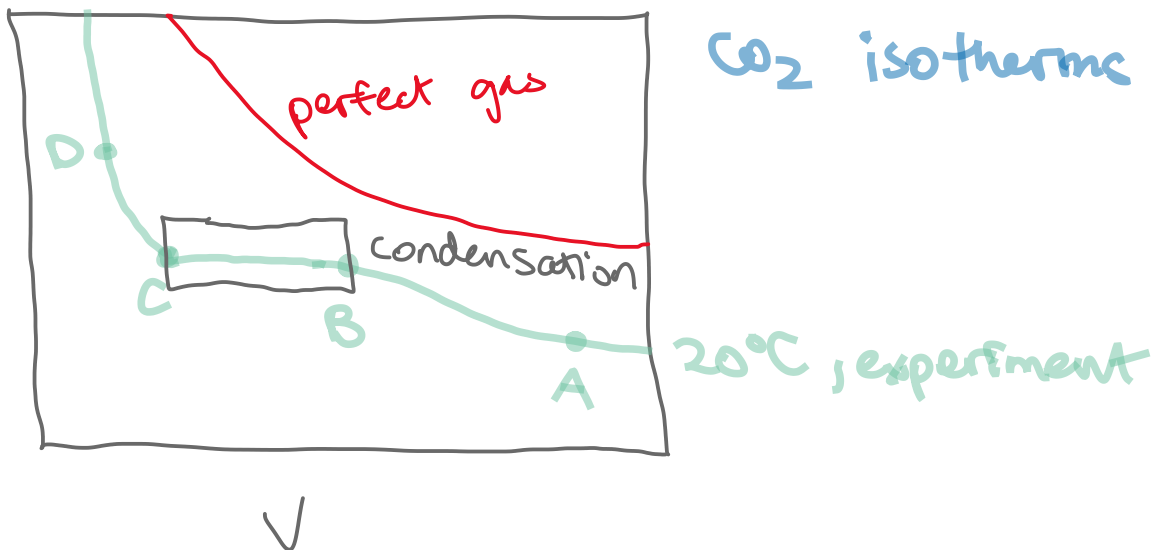
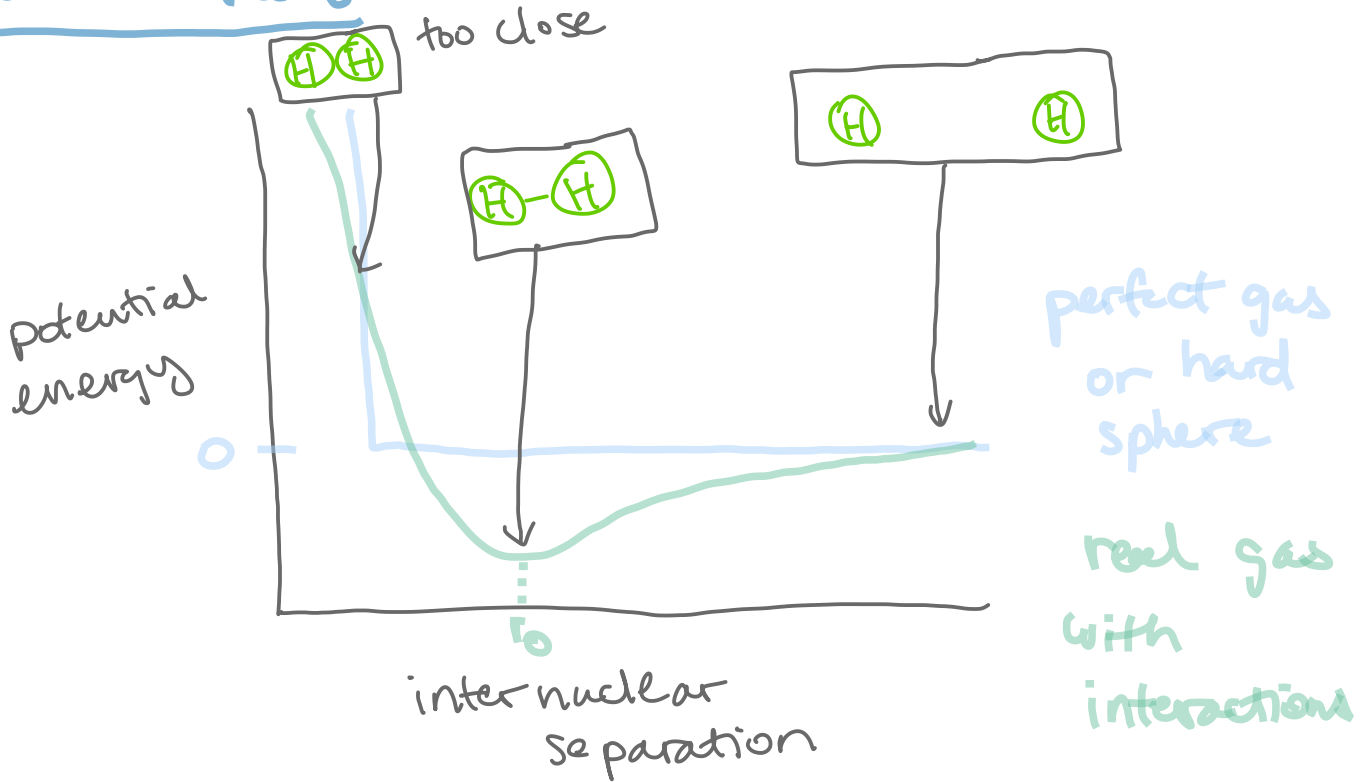
$$P_A + P_B + \dots = \underbrace{(x_A + x_B + \dots)}_{\text{sum of all mole fractions} = 1} P = P$$

sum of all
mole fractions = 1

Dalton's Law : the pressure exerted
by a mixture of gases is the sum

of the pressures that each one would exert if it occupied the container alone.
(perfect gases only)

Real Gases

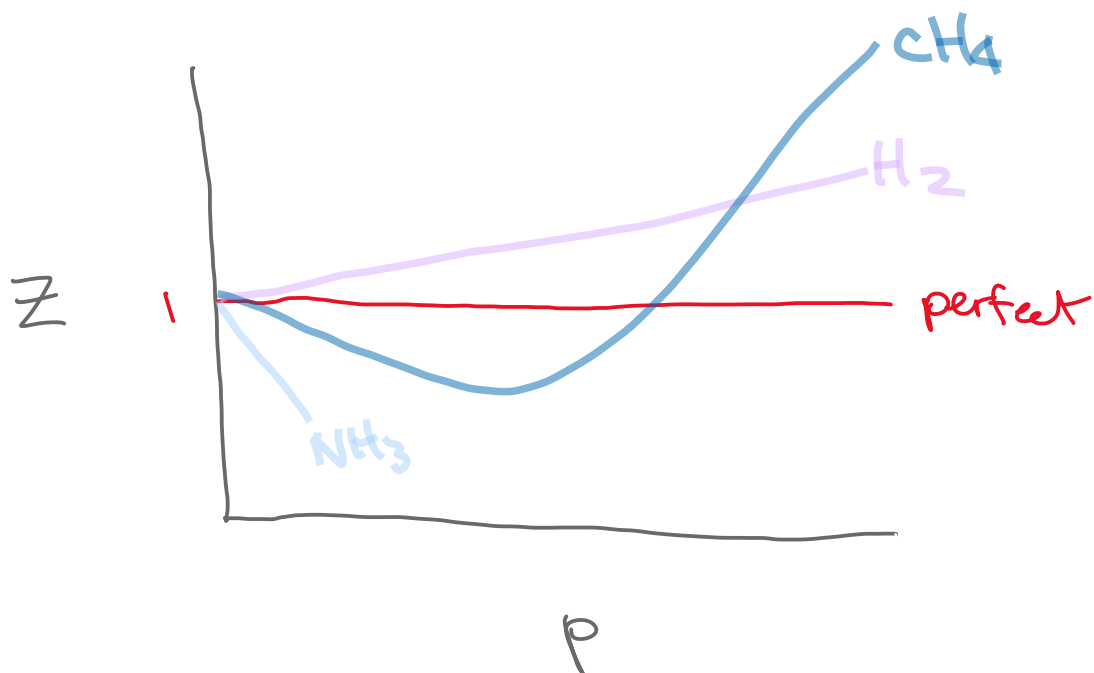


Compression Factor

$$Z = \frac{V_m}{V_m^{\circ}} \quad V_m^{\circ} = \frac{RT}{p}$$

$$Z = \frac{V_m}{RT/p} = \frac{pV_m}{RT}$$

$$pV_m = RTZ$$



How do we describe real gases more quantitatively?

... Z_r ...

$$P = \frac{nRT}{V}$$

$$P = \frac{nRT}{V-nb}$$

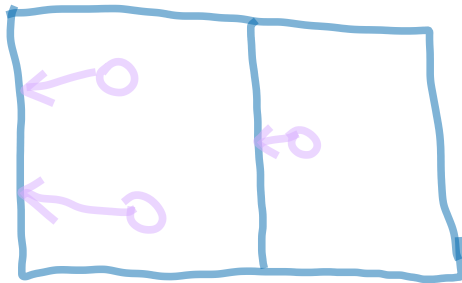
repulsive part



$$V_{\text{excluded}} = \frac{4}{3}\pi(2r)^3$$

$$V_{\text{excluded}} = 8V_{\text{molecule}}$$

per molecule:
4 V_{molecule}



before after

attractive part
reduces both the
frequency of collisions
as well as the force
of each collision

$$P = \frac{nRT}{V-nb} - a \frac{n^2}{V^2}$$

van der
Waals equation
of state

$$P = \frac{RT}{V_m - b} - \frac{a}{V_m^2}$$

alternate form

(a, b are arbitrary parameters)

